

## Osnovni trigonometrijski omjeri

Za pravokutni trokut:

- $\sin \alpha = \frac{\text{nasuprotna kateta}}{\text{hipotenuza}}$
- $\cos \alpha = \frac{\text{priležeća kateta}}{\text{hipotenuza}}$
- $\tan \alpha = \frac{\text{nasuprotna kateta}}{\text{priležeća kateta}} = \frac{\sin \alpha}{\cos \alpha}$
- $\cot \alpha = \frac{\text{priležeća kateta}}{\text{nasuprotna kateta}} = \frac{\cos \alpha}{\sin \alpha}$

## Formula za funkcije kuta od $90^\circ$ i $180^\circ$

- $\sin(90^\circ - \alpha) = \cos \alpha$
- $\cos(90^\circ - \alpha) = \sin \alpha$
- $\tan(90^\circ - \alpha) = \cot \alpha$
- $\cot(90^\circ - \alpha) = \tan \alpha$

## Dvostruki kutovi

- $\sin 2\alpha = 2 \sin \alpha \cos \alpha$
- $\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha = 2 \cos^2 \alpha - 1 = 1 - 2 \sin^2 \alpha$
- $\tan 2\alpha = \frac{2 \tan \alpha}{1 - \tan^2 \alpha}$

## Polovični kutovi

- $\sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$
- $\cos^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{2}$
- $\tan \frac{\alpha}{2} = \frac{\sin \alpha}{1 + \cos \alpha} = \frac{1 - \cos \alpha}{\sin \alpha}$

## Transformacija produkta u zbroj

- $\sin \alpha \cos \beta = \frac{1}{2} [\sin(\alpha + \beta) + \sin(\alpha - \beta)]$
- $\cos \alpha \cos \beta = \frac{1}{2} [\cos(\alpha + \beta) + \cos(\alpha - \beta)]$
- $\sin \alpha \sin \beta = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)]$

## Trigonometrijske funkcije u različitim kvadrantima

- I kvadrant:  $\sin > 0$ ,  $\cos > 0$ ,  $\tan > 0$ ,  $\cot > 0$
- II kvadrant:  $\sin > 0$ ,  $\cos < 0$ ,  $\tan < 0$ ,  $\cot < 0$
- III kvadrant:  $\sin < 0$ ,  $\cos < 0$ ,  $\tan > 0$ ,  $\cot > 0$
- IV kvadrant:  $\sin < 0$ ,  $\cos > 0$ ,  $\tan < 0$ ,  $\cot < 0$

## Pitagorin identitet

- $\sin^2 \alpha + \cos^2 \alpha = 1$
- $1 + \tan^2 \alpha = \frac{1}{\cos^2 \alpha}$
- $1 + \cot^2 \alpha = \frac{1}{\sin^2 \alpha}$

## Zbroj i razlika kuteva

- $\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$
- $\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$
- $\tan(\alpha \pm \beta) = \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta}$

## Funkcije negativnih kuteva

- $\sin(-\alpha) = -\sin \alpha$
- $\cos(-\alpha) = \cos \alpha$
- $\tan(-\alpha) = -\tan \alpha$
- $\cot(-\alpha) = -\cot \alpha$

## Radijani i stupnjevi

- Pretvaranje stupnjeva u radijane:  $\text{Radijani} = \frac{\pi}{180^\circ} \cdot \text{Stupnjevi}$
- Pretvaranje radijana u stupnjeve:  $\text{Stupnjevi} = \frac{180^\circ}{\pi} \cdot \text{Radijani}$

## Transformacija zbroja u produkt

- $\sin \alpha + \sin \beta = 2 \sin \frac{\alpha + \beta}{2} \cos \frac{\alpha - \beta}{2}$
- $\sin \alpha - \sin \beta = 2 \cos \frac{\alpha + \beta}{2} \sin \frac{\alpha - \beta}{2}$
- $\cos \alpha + \cos \beta = 2 \cos \frac{\alpha + \beta}{2} \cos \frac{\alpha - \beta}{2}$
- $\cos \alpha - \cos \beta = -2 \sin \frac{\alpha + \beta}{2} \sin \frac{\alpha - \beta}{2}$

### 1. Ako je poznato $\tan \alpha$ :

$$\cos^2 \alpha = \frac{1}{1 + \tan^2 \alpha}, \quad \sin^2 \alpha = \frac{\tan^2 \alpha}{1 + \tan^2 \alpha}$$

### 2. Ako je poznato $\sin \alpha$ :

$$\cos^2 \alpha = 1 - \sin^2 \alpha, \quad \tan \alpha = \frac{\sin \alpha}{\cos \alpha}, \quad \cot \alpha = \frac{\cos \alpha}{\sin \alpha}$$

### 3. Ako je poznato $\cos \alpha$ :

$$\sin^2 \alpha = 1 - \cos^2 \alpha, \quad \tan \alpha = \frac{\sin \alpha}{\cos \alpha}, \quad \cot \alpha = \frac{\cos \alpha}{\sin \alpha}$$

### 4. Ako je poznato $\cot \alpha$ :

$$\sin^2 \alpha = \frac{1}{1 + \cot^2 \alpha}, \quad \cos^2 \alpha = \frac{\cot^2 \alpha}{1 + \cot^2 \alpha}, \quad \tan \alpha = \frac{1}{\cot \alpha}$$

Kut ( $^\circ$ )	sin	cos	tan	cot
0 $^\circ$	0	1	0	$\infty$
30 $^\circ$	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{3}}{3}$	$\sqrt{3}$
45 $^\circ$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$	1	1
60 $^\circ$	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$	$\frac{\sqrt{3}}{3}$
90 $^\circ$	1	0	$\infty$	0
120 $^\circ$	$\frac{\sqrt{3}}{2}$	$-\frac{1}{2}$	$-\sqrt{3}$	$-\frac{\sqrt{3}}{3}$
135 $^\circ$	$\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{2}}{2}$	-1	-1
150 $^\circ$	$\frac{1}{2}$	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{3}}{3}$	$-\sqrt{3}$
180 $^\circ$	0	-1	0	$\infty$
210 $^\circ$	$-\frac{1}{2}$	$-\frac{\sqrt{3}}{2}$	$\frac{\sqrt{3}}{3}$	$\sqrt{3}$
225 $^\circ$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{2}}{2}$	1	1
240 $^\circ$	$-\frac{\sqrt{3}}{2}$	$-\frac{1}{2}$	$\sqrt{3}$	$\frac{\sqrt{3}}{3}$
270 $^\circ$	-1	0	$\infty$	0
300 $^\circ$	$-\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$-\sqrt{3}$	$-\frac{\sqrt{3}}{3}$
315 $^\circ$	$-\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$	-1	-1
330 $^\circ$	$-\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{3}}{3}$	$-\sqrt{3}$
360 $^\circ$	0	1	0	$\infty$